

## Field-dependent heat transport in the Kondo insulator $\text{SmB}_6$ : Phonons scattered by magnetic impurities

M-E. Boulanger,<sup>1</sup> F. Laliberté,<sup>1</sup> M. Dion,<sup>1</sup> S. Badoux,<sup>1</sup> N. Doiron-Leyraud,<sup>1</sup> W. A. Phelan,<sup>2,3</sup> S. M. Koohpayeh,<sup>3</sup> W. T. Fuhrman,<sup>3</sup> J. R. Chamorro,<sup>2,3</sup> T. M. McQueen,<sup>2,3,4</sup> X. F. Wang,<sup>5</sup> Y. Nakajima,<sup>5</sup> T. Metz,<sup>5</sup> J. Paglione,<sup>5,6</sup> and L. Taillefer<sup>1,6</sup>

<sup>1</sup>*Institut Quantique, Département de Physique and RQMP, Université de Sherbrooke, Sherbrooke, Québec, Canada J1K 2R1*

<sup>2</sup>*Department of Chemistry, Johns Hopkins University, Baltimore, Maryland 21218, USA*

<sup>3</sup>*Institute for Quantum Matter, Department of Physics and Astronomy, Johns Hopkins University, Baltimore, Maryland 21218, USA*

<sup>4</sup>*Department of Materials Science and Engineering, Johns Hopkins University, Baltimore, Maryland 21218, USA*

<sup>5</sup>*Center for Nanophysics and Advanced Materials, Department of Physics, University of Maryland, College Park, Maryland 20742, USA*

<sup>6</sup>*Canadian Institute for Advanced Research, Toronto, Ontario, Canada M5G 1Z8*



(Received 29 September 2017; published 25 June 2018)

The thermal conductivity  $\kappa$  of the Kondo insulator  $\text{SmB}_6$  was measured at low temperature, down to 70 mK, in magnetic fields up to 15 T, on single crystals grown using both the floating-zone and the flux methods. The residual linear term  $\kappa_0/T$  at  $T \rightarrow 0$  is found to be zero in all samples, for all magnetic fields, in agreement with previous studies. There is therefore no clear evidence of fermionic heat carriers. In contrast to some prior data, we observe a large enhancement of  $\kappa(T)$  with increasing field. The effect of field is anisotropic, depending on the relative orientation of field and heat current (parallel or perpendicular), and with respect to the cubic crystal structure. We interpret our data in terms of heat transport predominantly by phonons, which are scattered by magnetic impurities.

DOI: [10.1103/PhysRevB.97.245141](https://doi.org/10.1103/PhysRevB.97.245141)

### I. INTRODUCTION

Samarium hexaboride ( $\text{SmB}_6$ ) is a Kondo insulator, a material in which the interaction between the localized  $f$  electrons and the conduction band gives rise to a hybridized band structure with a gap [1]. The correlated metallic behavior at high temperature smoothly becomes insulating below 40 K with the opening of the Kondo gap, giving rise to a diverging resistance at low temperature. However, below  $\sim 5$  K, a resistivity plateau is observed, the signature of a metallic state at the surface of the sample [2–7]. This surface state may be topological in nature.

Recently, two independent studies [8,9] reported the observation of de Haas–van Alphen (dHvA) oscillations in  $\text{SmB}_6$ , but with different interpretations. In the first, Li *et al.* attributed the quantum oscillations to a two-dimensional Fermi surface associated with the metallic surface state [8]. In the second, Tan *et al.* detected additional frequencies and attributed the quantum oscillations to a three-dimensional Fermi surface associated with the insulating bulk [9]. Although it has been shown that dHvA oscillations can indeed occur in a band insulator like  $\text{SmB}_6$  [10], a more exotic possibility is the existence of neutral fermions.

One way to detect mobile fermions is through their ability to carry entropy, which a measurement of the thermal conductivity  $\kappa(T)$  should in principle detect as a nonzero residual linear term in the  $T = 0$  limit, i.e.,  $\kappa_0/T > 0$ . In this paper, we report low-temperature thermal conductivity measurements in high-quality single crystals of  $\text{SmB}_6$  down to 70 mK. In agreement with a prior study [11], we observe no residual linear term  $\kappa_0/T$ , at any value of the magnetic field up to 15 T. However, unlike in that prior study, we observe

a large field-induced enhancement of  $\kappa(T)$ . There are two general scenarios for this: either magnetic excitations (like magnons or spinons) carry heat, or phonons are scattered by a field-dependent mechanism, like magnetic impurities or spin fluctuations. In this paper, we argue that our data on  $\text{SmB}_6$  are consistent with the latter scenario, and discuss in particular the case of phonons scattered by magnetic impurities.

### II. METHODS

We studied six single crystals of  $\text{SmB}_6$ , four grown at Johns Hopkins University by the floating-zone method (labeled Z1, Z2, and ZC) and by the flux method (F3), and two grown at University of Maryland by the flux method (labeled F1 and F2). Growth methods are described elsewhere [12–15]. Sample Z1 was prepared using in-house sources of samarium and boron, while samples Z2 and ZC were prepared using commercial sources. (“C” here refers to carbon doping, in a fraction that is virtually impossible to know precisely [7,12], but presumed to be at the 1–5% level). The two types of starting material imply different concentrations of rare-earth impurities. The former predominantly contain Gd impurities [13], while the latter have more nonmagnetic than magnetic impurities. In addition, samples contain Sm vacancies, typically at the 1% level. Such vacancies are known to enhance the valence of Sm in  $\text{SmB}_6$  from the nonmagnetic  $\text{Sm}^{2+}$  valence to the  $J = 5/2$  magnetic  $\text{Sm}^{3+}$ , possibly acting like magnetic impurities [16]. Surface and bulk magnetic properties of  $\text{Sm}^{2+}$  and  $\text{Sm}^{3+}$  were recently studied using x-ray-absorption spectroscopy and x-ray magnetic circular dichroism on a sample directly comparable to Z2 [17], giving insight on the coupling to magnetic impurities. The samples were cut in the shape of rectangular

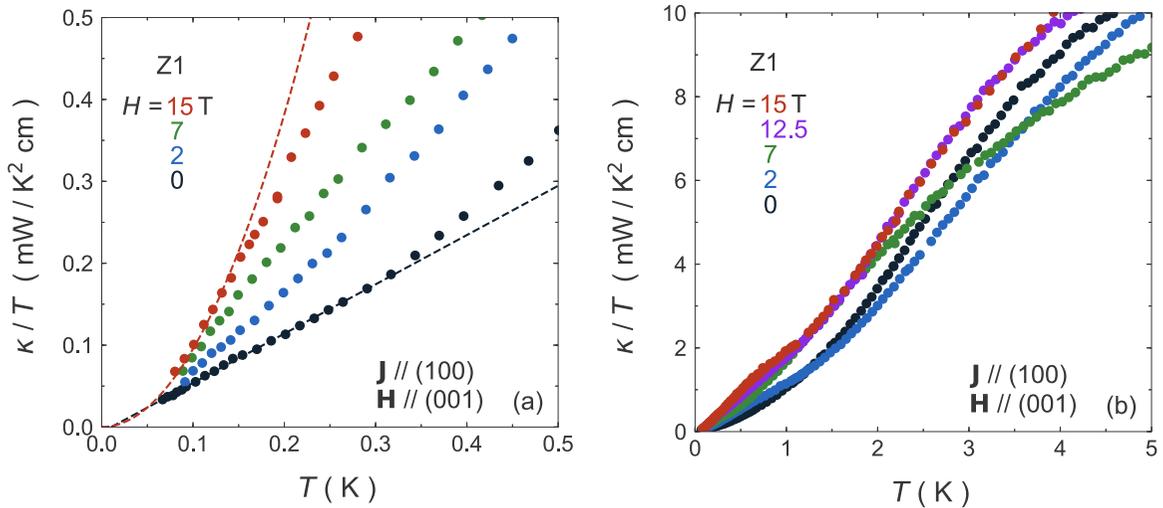


FIG. 1. Thermal conductivity of  $\text{SmB}_6$  plotted as  $\kappa/T$  vs  $T$  for various values (as indicated) of the magnetic field applied perpendicular to the heat current,  $\mathbf{H} // (001)$  and  $\mathbf{J} // (100)$ . (a) Low-temperature regime ( $T < 0.5$  K). The black dashed line is a linear fit to the zero-field data below 0.3 K. The red dashed line is  $\kappa = \beta T^3$ , with  $\beta = 9.5 \text{ mW/K}^4 \text{ cm}$ , showing that the 15 T data are consistent with  $\kappa/T \sim T^2$  below 0.15 K. Although the field enhances  $\kappa(T)$  significantly, there is no residual linear term at any field, i.e.,  $\kappa/T \rightarrow 0$  as  $T \rightarrow 0$ . (b) High-temperature regime. The field dependence of  $\kappa(T)$  is nonmonotonic.

platelets with the following dimensions (length  $\times$  width  $\times$  thickness, in  $\mu\text{m}$ ): 1650  $\times$  450  $\times$  300 (Z1), 1480  $\times$  730  $\times$  218 (Z2), 1460  $\times$  1330  $\times$  210 (ZC), 1375  $\times$  780  $\times$  290 (F1),

990  $\times$  830  $\times$  218 (F2), and 2930  $\times$  830  $\times$  405 (F3). The contacts were made using H20E silver epoxy. Room-temperature resistivities were 0.23, 0.22, 0.23, 0.18, and 0.16  $\text{m}\Omega \text{ cm}$  for

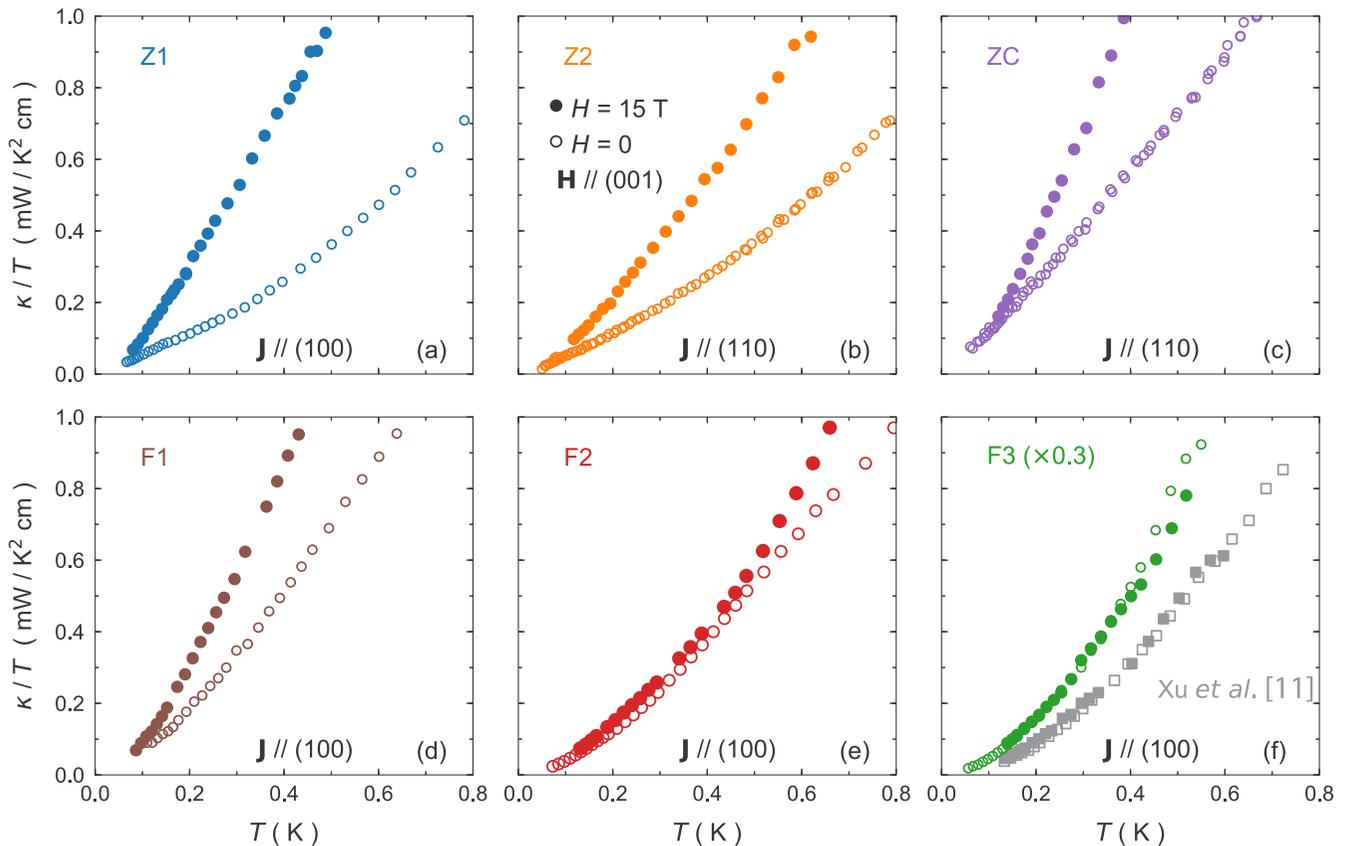


FIG. 2. Thermal conductivity of our three zone-grown (upper panels) and flux-grown (lower panels) samples of  $\text{SmB}_6$ , plotted as  $\kappa/T$  vs  $T$  for  $H = 0$  (open circles) and  $H = 15$  T [full circles;  $\mathbf{H} // (001)$ ]. In panel (f), we reproduce the data by Xu *et al.* [11] taken on a flux-grown sample ( $H = 0$ , open squares;  $H = 14.5$  T, full squares) and compare them with our own flux-grown sample F3 (multiplied by 0.3).

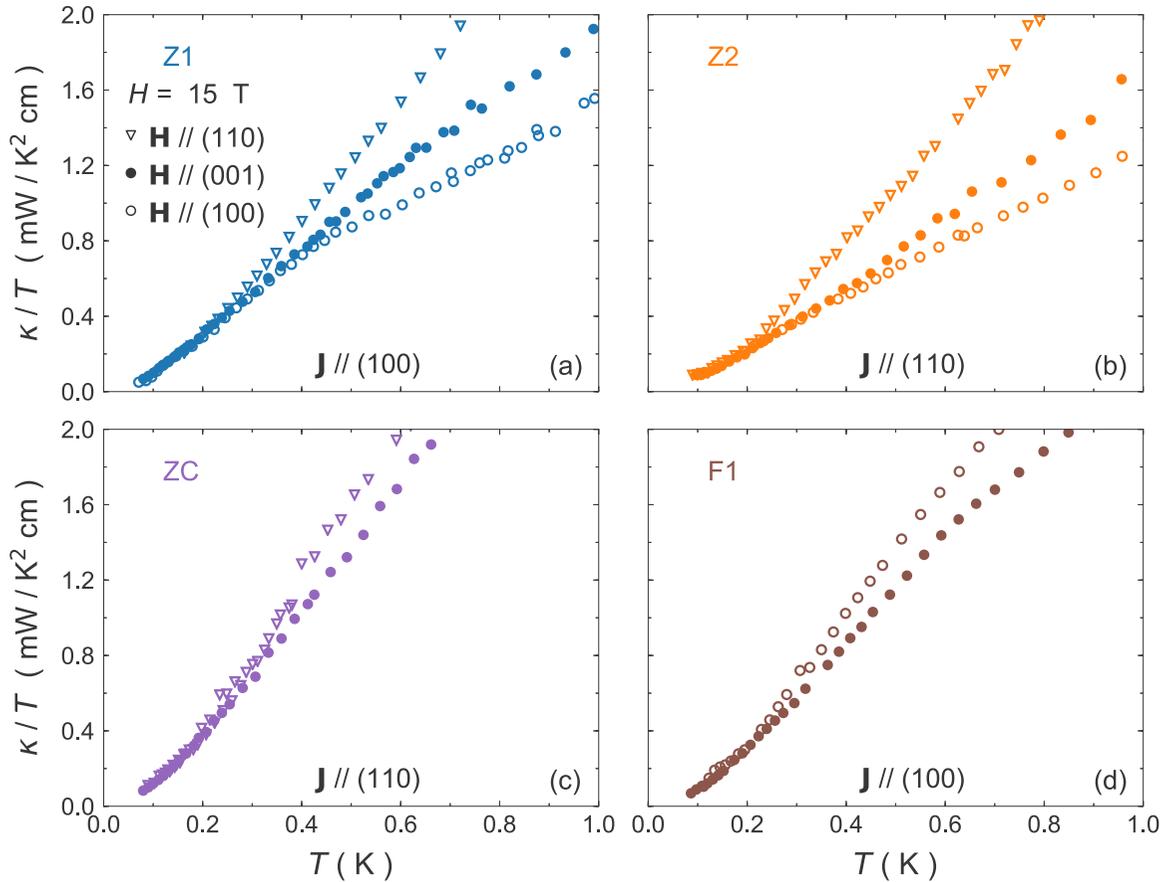


FIG. 3. Anisotropy of thermal conductivity at  $H = 15$  T, for a field applied in different directions (as indicated) with respect to the crystal structure axes. Note that the data are isotropic at the lowest temperatures and no clear pattern of anisotropy emerges.

Z1, Z2, ZC, F1, and F2, respectively. Contact resistances were between  $100 \Omega$  and  $2 \text{ k}\Omega$ . The relative orientation between the crystal structure and the sample dimensions was determined via x-ray-diffraction measurements primarily using diffraction peaks (001) and (103). These measurements also revealed the samples to be good quality single crystals. The thermal conductivity was measured in a dilution refrigerator down to  $70 \text{ mK}$  with a standard one-heater two-thermometers technique with the heat flowing along the longest dimension. The current was injected along the (100) high-symmetry direction of the cubic crystal structure, i.e.,  $\mathbf{J} // (100)$ , for Z1, F1, F2, and F3, and along (110) for Z2 and ZC.

Note that the conductivity of the metallic surface state makes a completely negligible contribution to the sample's thermal conductivity, so the measured  $\kappa(T)$  is strictly a property of the insulating bulk. Indeed, given that the low- $T$  resistivity plateau ranges between  $10^{-2}$  and  $10^0 \Omega \text{ cm}$  for our samples, and using the Wiedemann-Franz law  $\kappa_0/T = L_0/\rho_0$  where  $L_0 = 2.44 \times 10^{-8} \text{ W } \Omega \text{ K}^{-2}$ , we expect a contribution from the metallic surface state between  $10^{-3}$  and  $10^{-5} \text{ mW/K}^2 \text{ cm}$ .

### III. RESULTS

In Fig. 1, the thermal conductivity of sample Z1 is plotted as  $\kappa/T$  versus  $T$ , for various values of the field applied

perpendicular to the heat current ( $\mathbf{H} \perp \mathbf{J}$ ). At  $T > 2 \text{ K}$ , the effect of the field is nonmonotonic:  $\kappa(T)$  decreases with  $H$  at first, and then increases. At  $T < 0.5 \text{ K}$  [Fig. 1(a)], the behavior is simpler: the magnetic field enhances  $\kappa(T)$ . This is true for our three zone-grown samples, as shown in Fig. 2. A comparable effect is observed for our flux-grown sample F1, but the enhancement is much smaller for F2 and negligible for F3. This last result is similar to the previous study by Xu *et al.* [11], performed on a flux-grown crystal [see Fig. 2(f)]. This sample dependence suggests that an extrinsic mechanism is responsible for the field enhancement.

To examine whether part of the heat transport in  $\text{SmB}_6$  is carried by fermionic particles, we first look for a residual linear term. Simple extrapolation of the data in Fig. 1(a) yields  $\kappa_0/T = 0$  at all fields. The same is true for all samples (Fig. 2), as also found by Xu *et al.* [11]. Indeed, a linear fit to  $\kappa/T$  versus  $T$  at  $H = 0$  describes the data well below  $0.3 \text{ K}$ , but it yields a negative value for  $\kappa_0/T$ . This means that  $\kappa/T$  must go over to a higher power of  $T$  at very low  $T$ , as expected for phonon conduction, which must go as  $\kappa_p/T \sim T^2$  in the limit  $T \rightarrow 0$ . Moreover, the large enhancement with field does not generate a residual linear term. Indeed, the data at  $H = 15 \text{ T}$  also extrapolate to zero as  $T \rightarrow 0$ , and are consistent with  $\kappa/T \sim T^2$  below  $0.15 \text{ K}$ . Because  $\kappa_0/T = 0$  in all samples at all fields, we are left with no direct evidence of fermionic

carriers of heat. Note, however, that we cannot entirely exclude them, as they could be present but thermally decoupled from the phonons that bring the heat into the sample [18].

In Fig. 3, the low-temperature thermal conductivity at  $H = 15$  T is shown for different field directions with respect to the crystal structure axes. At the lowest temperatures, the effect of a field is isotropic. However, above a certain temperature (between 0.2 and 0.4 K), an anisotropy develops. The anisotropy was observed in all floating-zone samples, but only in flux-grown sample F1. For floating-zone samples, in all cases, the largest conductivity is achieved when the field is aligned with (110). For Z2 and ZC, this occurs when the field is applied parallel to the heat current, but for Z1 (110) is at  $45^\circ$  with respect to the heat current. For both Z1 and Z2, the conductivity is smallest when the field is along (100), regardless of the heat current direction. On the other hand, the anisotropy of sample F1 is reversed, i.e., the conductivity is largest when the field is along (100), which is also the heat current direction in this case. Globally, considering all four samples where an anisotropy is observed, there seems to be no systematic tendency. However, among floating-zone samples, the behavior is the same with respect to the crystal axes.

#### IV. DISCUSSION

Here we discuss a possible scenario for the complex behavior of heat transport in  $\text{SmB}_6$ , where we take the conservative view that the heat is carried entirely by phonons. The question is what scatters those phonons. In the absence of electrons, since  $\text{SmB}_6$  is a bulk insulator, there are two kinds of scattering processes. The first kind is independent of magnetic field. It includes sample boundaries, dislocations, grain boundaries, vacancies, and nonmagnetic impurities. Now because  $\kappa$  in  $\text{SmB}_6$  is strongly field dependent, there must be a second kind of scattering process, which depends on field, involving either low-energy magnetic excitations, such as magnons, or magnetic impurities. Recent experiments suggest the existence of intrinsic subgap excitations, in the form of either bosonic excitations as observed via inelastic neutron scattering [19] or persistent spin dynamics that extend to very low temperatures as measured in muon spin-relaxation experiments [15].

Because  $\text{SmB}_6$  samples are known to contain significant levels of rare-earth impurities and Sm vacancies, phonons are certainly scattered by those impurities. Even at the 1% level, magnetic impurities can cause a major suppression of the phonon thermal conductivity in insulators at low temperature [20]. Phonons will scatter most strongly when their energy matches the difference between the atomic energy levels of the impurity. Applying a magnetic field will split some of those energy levels. Increasing the field can therefore make phonons at low  $T$  less and less scattered. This is our proposal for why  $\kappa$  in  $\text{SmB}_6$  increases with field at low  $T$ .

With decreasing temperature, when the phonon mean free path grows to reach the sample dimensions, it becomes constant and equal to  $\ell_0 = 2\sqrt{A/\pi}$ , where  $A$  is the cross-sectional area of the sample. [This is strictly true only for scattering off rough surfaces. Smooth surfaces can cause specular reflection of phonons, yielding a temperature-dependent (wavelength-dependent) mean free path that exceeds the sample dimensions [21].]

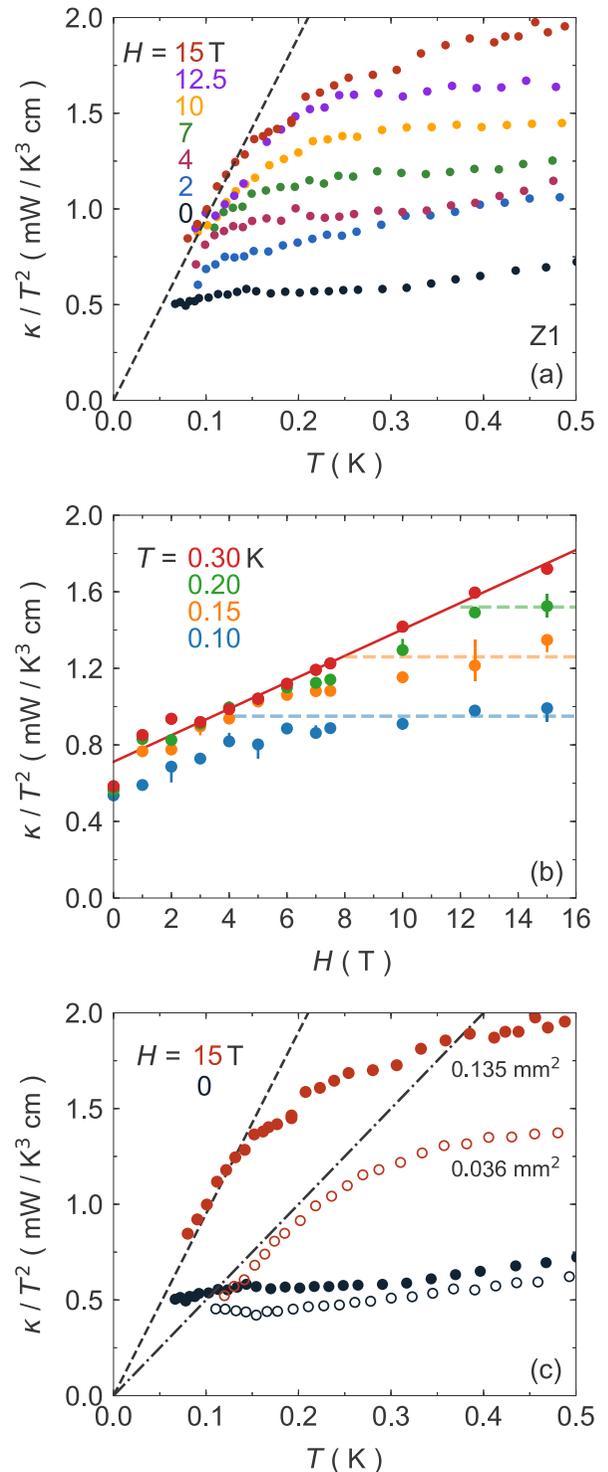


FIG. 4. (a) Same data as in Fig. 1(a), plotted as  $\kappa/T^2$  vs  $T$ . The black dashed line is  $\kappa = \beta T^3$ , with  $\beta = 9.5$  mW/K<sup>4</sup> cm. (b) Same data, plotted as  $\kappa/T^2$  vs  $H$ , for four temperatures as indicated. All lines are guides to the eye. The red line shows how the data at 0.3 K rise linearly up to the highest field. The blue line shows how the data at 0.1 K saturate above  $H \approx 6$  T, to a value consistent with  $\beta = 9.5$  mW/K<sup>4</sup> cm. (c) Same data at 0 and 15 T from panel (a), compared to the data obtained after polishing the Z1 sample, reducing the cross-sectional area (width and thickness) by a factor 3.7 (open circles). The dot-dashed line is the same as the dashed line, but this slope is reduced by a factor  $\sqrt{3.7}$ , as expected from Eq. (1).

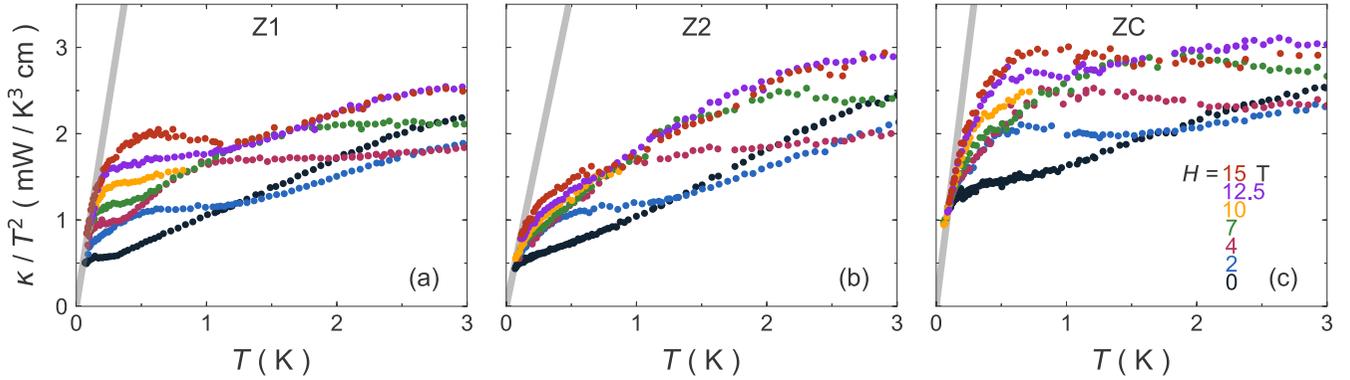


FIG. 5. Thermal conductivity of samples Z1 (a), Z2 (b), and ZC (c) plotted as  $\kappa/T^2$  vs  $T$  up to 3 K and for various magnetic field applied perpendicular to the heat current. The gray line in each panel shows the estimated boundary-limited phonon contribution, calculated using Eq. (1) and the appropriate sample dimensions.

In that regime, the phonon thermal conductivity is given by [21]

$$\kappa_p(T) = \frac{2}{15} \pi^2 k_B \left( \frac{k_B T}{\hbar} \right)^3 v_p^{-2} \ell_0 \quad (1)$$

where  $v_p^{-2}$  is the inverse square of the sound velocity averaged over three acoustic branches in all  $\mathbf{q}$  directions.

An estimate of the appropriate mean sound velocity may be obtained in terms of the longitudinal ( $v_L$ ) and transverse sound velocities ( $v_{T1}$  and  $v_{T2}$ ) [21]:

$$\frac{3}{v_p^2} = \frac{1}{v_L^2} + \frac{1}{v_{T1}^2} + \frac{1}{v_{T2}^2}. \quad (2)$$

Using the elastic constants of SmB<sub>6</sub> measured at low temperature [22], we have  $v_L = 7350$  m/s,  $v_{T1} = 3580$  m/s, and  $v_{T2} = 6670$  m/s, giving  $v_p \simeq 5000$  m/s. Similar values of  $v_p$  can be obtained using the Debye temperature  $\Theta_D = 373$  K [23] or other estimates [24].

Given the dimensions of sample Z1,  $\ell_0 = 0.42$  mm, our estimate of the boundary-limited phonon conductivity is  $\kappa_p(T) = \beta T^3$  with  $\beta = 7 \pm 1$  mW/K<sup>4</sup> cm, where the error bar reflects the uncertainty on  $v_p$  and on sample dimensions. In Figs. 1(a) and 4(a), we see that the data for sample Z1 at  $H = 15$  T are consistent with  $\kappa = \beta T^3$  below 0.15 K, with  $\beta \simeq 9$  mW/K<sup>4</sup> cm, a value close to our estimate from Eq. (1). At  $H = 0$ , however,  $\kappa(T)$  is well below that. Our hypothesis is that a magnetic scattering process present in zero field lowers  $\kappa$  in SmB<sub>6</sub>, and this process is quenched or gapped by a field, until it is essentially inactive at  $H > 15$  T.

To explore this further, we plot the data as  $\kappa/T^2$  versus  $T$  in Fig. 4(a). We see that all curves lie below an upper bound given by the straight line  $\kappa/T^2 = \beta T$  with  $\beta \simeq 9$  mW/K<sup>4</sup> cm. As seen from the data plotted as  $\kappa/T^2$  versus  $H$  in Fig. 4(b), at  $T = 0.1$  K the field increases  $\kappa$  until it reaches this line, at  $H \simeq 6$  T, above which it saturates. At  $T = 0.2$  K, saturation occurs above  $H \simeq 12$  T [Fig. 4(b)]. This behavior is consistent with a scattering process that is gapped by the field.

To test this interpretation, we reduced the cross-sectional area of the Z1 sample by a factor 3.7 (the width was reduced from 450 to 315  $\mu\text{m}$ , and the thickness was reduced from 300 to 115  $\mu\text{m}$ ), implying that the boundary-limited phonon conductivity is smaller by a factor  $\sqrt{3.7}$ . This is indeed what is

observed in Fig. 4(c), confirming our conclusion that the low  $T$  thermal conductivity is set by the boundary limit once the applied magnetic field has gapped the scattering mechanism present in zero field.

As seen in Fig. 5, the same situation is observed in our three floating zone samples, whereby  $\kappa(T)$  at low  $T$  is confined below  $\kappa = \beta T^3$ , where  $\beta$  is consistent with the value estimated from Eq. (1) given the particular sample dimensions.

We have focused so far on the low-temperature regime below 0.3 K or so. At higher temperatures, there is a strong but complex field dependence of  $\kappa(T)$ , as seen in Figs. 1(b) and 5. In order to make sense of it, it is instructive to look at the incremental effect of increasing the field by 1 T, as a function of temperature up to 5 K. This is shown in Fig. 6(a). The difference between  $\kappa(H)$  and  $\kappa(H - 1)$  reveals a peak at some temperature. As we increase the field, the peak moves up to higher and higher temperature. In Fig. 6(b), the peak position is seen to scale with  $H$  in a roughly linear manner. This is again consistent with a scenario of magnetic scattering being gapped by the field, with the gap growing with  $H$ . Note, however, that we are now dealing with phonons of much higher energy than before.

It is interesting to look at the energy scales. Given that the phonons which dominate the thermal conductivity have an energy  $E_{\text{ph}} \sim 4k_B T$ , Fig. 6(b) tells us that those phonons are scattered by some mechanism, the characteristic energy of which is  $\Delta \simeq 2\mu_B H$ . If the scattering is associated with the Zeeman splitting of atomic levels, so that  $\Delta = 2gJ\mu_B H$ , we get  $gJ \simeq 1$  from the condition  $E_{\text{ph}} = \Delta$ , close to the value of  $gJ$  for Sm<sup>3+</sup> vacancies.

One of the most puzzling features of the field dependence is its anisotropy relative to the cubic crystal structure axes. For floating-zone samples,  $\kappa$  is largest for the field parallel to (110), intermediate for (001), and smallest for (100). This is true whether the heat current is along (100) or along (110). For flux sample F1, the anisotropy is reversed: largest for (100) and smallest for (001). It is difficult to explain the anisotropy given the lack of uniform trend. One possibility is that the scattering of phonons by magnetic impurities changes as the field direction changes. In this scenario, the variation in composition between floating-zone and flux-grown samples could explain the opposite behavior of F1 [12,13]. A theoretical

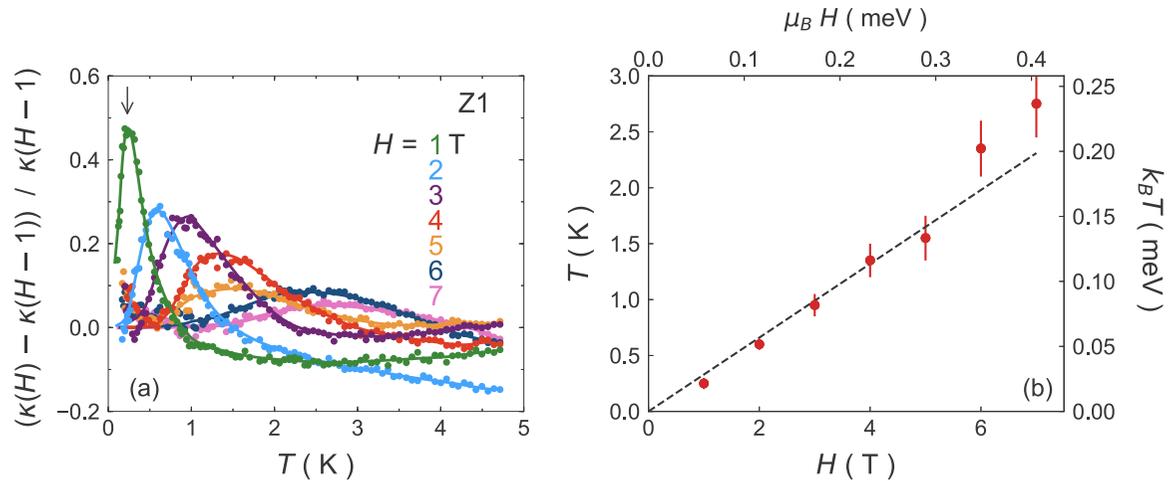


FIG. 6. (a) Normalized difference between two temperature dependencies for the Z1 sample measured at two consecutive magnetic fields, with field applied perpendicular to the heat current. A maximum in the difference (e.g., vertical arrow for 1 T) is observed at a temperature that scales with magnetic field. (b) The temperature of that maximum as a function of magnetic field. All lines are guides to the eye.

model is needed to understand our observation, which is beyond the scope of this paper. Note that below a certain temperature—0.4 K for one field orientation and 0.2 K for the other—there is no anisotropy at  $H = 15$  T (Fig. 3). This is consistent with our interpretation that once the field has gapped the magnetic scattering process the phonon mean free path becomes independent of field as it is limited by the sample boundaries, irrespective of the field orientation.

In summary, we propose that rare-earth impurities in  $\text{SmB}_6$ , including Sm vacancies, known to be present at significant levels in even the best samples [13], scatter phonons, and this scattering process is suppressed by a magnetic field, at low temperature. Theoretical calculations are needed to understand the temperature and field dependence, as well as the anisotropy of the process.

Lastly, we discuss a recent study by Hartstein *et al.* on floating-zone grown samples [25]. They report a substantial field-induced enhancement of  $\kappa(T)$  (well below the charge gap energy scale) which they interpret as evidence for a Fermi surface in the bulk arising from novel itinerant low-energy excitations. This is a very different interpretation to the one we propose here. In zero field, their data at low  $T$  are well described by Eq. (1), i.e.,  $\kappa/T$  goes as  $T^2$  with an amplitude expected from their sample's dimensions. Applying a field then increases  $\kappa(T)$  beyond the phonon amplitude predicted by the boundary limit, which they interpret as a fermionic contribution. Note, however, that having a purely phononic  $\kappa(T)$  larger than the value predicted by Eq. (1) is not impossible. Indeed, the boundary limit applies when phonon reflections on the surfaces are diffusive. If reflections are specular, the mean free path is not limited by the sample's boundaries, which makes the temperature dependence of  $\kappa(T)$  smaller than  $T^3$  and its amplitude larger than in the diffusive case [21].

In comparison, our zero-field data are well below the boundary limit. This reveals that their sample is of higher quality, implying longer phonon mean free paths. But despite the variation in sample quality, the effect of magnetic field is comparable. In Fig. 7, we plot the difference between  $\kappa(T)/T$  at 15 T and at zero field for our three floating-zone samples,

along with the same difference for their sample (with 12 T). The enhancement in field is comparable in the sense that it grows smoothly as a function of temperature, but apparently with an offset of about  $0.2 \text{ mW/K}^2 \text{ cm}$  in their data. In contrast to their data, it is unambiguous from our data that  $\Delta\kappa/T$  extrapolates to zero as  $T \rightarrow 0$ , in agreement with our conclusion that no residual linear term is observed at any field.

If the enhancement in thermal conductivity were really caused by field-induced low-energy fermionic excitations, there should be a residual linear term. By measuring at much lower temperature, we confirm that  $\kappa_0/T \rightarrow 0$  even in 15 T. Moreover, such speculated fermionic excitations would lead to a rapid downturn at low temperature due to phonon decoupling. Since neither of these two signatures is observed, we conclude that there is no experimental evidence of bulk Fermi surfaces in the thermal conductivity of  $\text{SmB}_6$ .

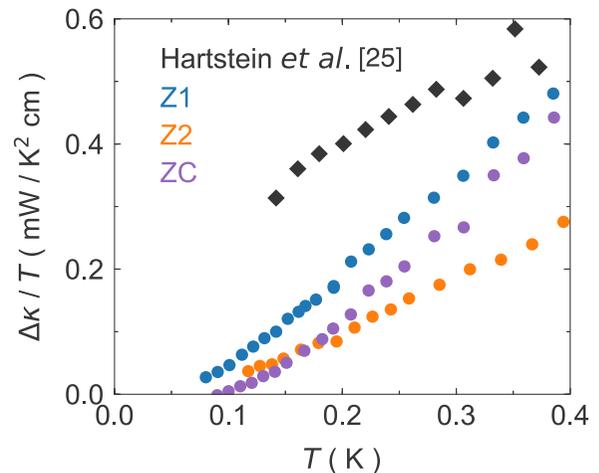


FIG. 7. Field-induced thermal conductivity enhancement at low  $T$  for the zone-grown samples, plotted as  $\Delta\kappa/T = [\kappa(H_{\text{max}}) - \kappa(0)]/T$  vs  $T$ , where  $H_{\text{max}} = 15$  T for Z1, Z2, and ZC, and 12 T for the sample of Ref. [25] (black diamonds).

## V. SUMMARY

We have measured the thermal conductivity of  $\text{SmB}_6$  down to 70 mK, in three zone-grown and three flux-grown crystals. No residual linear term was observed in any sample, either in zero field or in any field up to 15 T. This means that there is no concrete evidence of fermionic heat carriers in  $\text{SmB}_6$ . However, the field produces a significant enhancement of  $\kappa(T)$  in most samples.

We interpret our data in a scenario where phonons are the only carriers of heat, and they are scattered by a magnetic mechanism that is gapped by the field, such that by 15 T the phonon mean free path grows to reach the sample boundaries at the lowest temperatures. The fact that the effect of field depends on its orientation relative to the crystal structure points to an extrinsic mechanism. We propose that phonons are scattered by magnetic rare-earth impurities or vacancies. The fact that the field-induced enhancement of  $\kappa(T, H)$  shifts linearly to higher  $T$  with increasing  $H$  is consistent with the Zeeman splitting of atomic levels responsible for the impurity scattering.

## ACKNOWLEDGMENTS

We acknowledge valuable discussions with P. Coleman, J. Knolle, S. Y. Li, J.-Ph. Reid, M. Sutherland, and W. Toews. We thank S. Fortier for his assistance with the experiments. L.T. acknowledges support from the Canadian Institute for Advanced Research and funding from the Institut Quantique, the Natural Sciences and Engineering Research Council of Canada (Grant No. PIN:123817), the Fonds de Recherche en Nature et Technologies, the Canada Foundation for Innovation, and a Canada Research Chair. Research at the University of Maryland was supported by AFOSR through Grant No. FA9550-14-1-0332 and the Gordon and Betty Moore Foundation's EPIQS Initiative through Grant No. GBMF4419. Work at the Institute for Quantum Matter was supported by the U.S. Department of Energy, Office of Basic Energy Sciences, Division of Materials Sciences and Engineering through Grant No. DE-FG02-08ER46544. Partial funding for this work was provided by the Johns Hopkins University Catalyst Fund.

- 
- [1] M. Dzero, K. Sun, V. Galitski, and P. Coleman, *Phys. Rev. Lett.* **104**, 106408 (2010).
- [2] N. Xu, X. Shi, P. K. Biswas, C. E. Matt, R. S. Dhaka, Y. Huang, N. C. Plumb, M. Radović, J. H. Dil, E. Pomjakushina *et al.*, *Phys. Rev. B* **88**, 121102 (2013).
- [3] D. J. Kim, S. Thomas, T. Grant, J. Botimer, Z. Fisk, and J. Xia, *Sci. Rep.* **3**, 3150 (2013).
- [4] M. M. Yee, Y. He, A. Soumyanarayanan, D.-J. Kim, Z. Fisk, and J. E. Hoffman, [arXiv:1308.1085](https://arxiv.org/abs/1308.1085) (2013).
- [5] X. Zhang, N. P. Butch, P. Syers, S. Ziemak, R. L. Greene, and J. Paglione, *Phys. Rev. X* **3**, 011011 (2013).
- [6] S. Wolgast, C. Kurdak, K. Sun, J. W. Allen, D.-J. Kim, and Z. Fisk, *Phys. Rev. B* **88**, 180405 (2013).
- [7] W. A. Phelan, S. M. Koohpayeh, P. Cottingham, J. W. Freeland, J. C. Leiner, C. L. Broholm, and T. M. McQueen, *Phys. Rev. X* **4**, 031012 (2014).
- [8] G. Li, Z. Xiang, F. Yu, T. Asaba, B. Lawson, P. Cai, C. Tinsman, A. Berkley, S. Wolgast, Y. S. Eo *et al.*, *Science* **346**, 1208 (2014).
- [9] B. Tan, Y.-T. Hsu, B. Zeng, M. Ciomaga Hatnean, N. Harrison, Z. Zhu, M. Hartstein, M. Kiourlappou, A. Srivastava, M. D. Johannes *et al.*, *Science* **349**, 287 (2015).
- [10] J. Knolle and N. R. Cooper, *Phys. Rev. Lett.* **115**, 146401 (2015).
- [11] Y. Xu, S. Cui, J. K. Dong, D. Zhao, T. Wu, X. H. Chen, K. Sun, H. Yao, and S. Y. Li, *Phys. Rev. Lett.* **116**, 246403 (2016).
- [12] W. A. Phelan, S. M. Koohpayeh, P. Cottingham, J. A. Tutmaher, J. C. Leiner, M. D. Lumsden, C. M. Lavelle, X. P. Wang, C. Hoffmann, M. A. Siegler *et al.*, *Sci. Rep.* **6**, 20860 (2016).
- [13] W. T. Fuhrman, J. R. Chamorro, P. Alekseev, J.-M. Mignot, T. Keller, J. Rodriguez-Rivera, Y. Qiu, P. Nikolic, T. M. McQueen, and C. L. Broholm, *Nat. Commun.* **9**, 1539 (2018).
- [14] P. Syers, D. Kim, M. S. Fuhrer, and J. Paglione, *Phys. Rev. Lett.* **114**, 096601 (2015).
- [15] K. Akintola, A. Pal, M. Potma, S. R. Saha, X. F. Wang, J. Paglione, and J. E. Sonier, *Phys. Rev. B* **95**, 245107 (2017).
- [16] E. Konovalova, *Sov. Powder Metall. Met. Ceram.* **21**, 820 (1982).
- [17] W. T. Fuhrman, J. C. Leiner, J. Freeland, M. van Veenendaal, S. M. Koohpayeh, W. A. Phelan, T. M. McQueen, and C. Broholm, [arXiv:1804.06853](https://arxiv.org/abs/1804.06853) (2018).
- [18] M. F. Smith, J. Paglione, M. B. Walker, and L. Taillefer, *Phys. Rev. B* **71**, 014506 (2005).
- [19] W. T. Fuhrman, J. Leiner, P. Nikolić, G. E. Granroth, M. B. Stone, M. D. Lumsden, L. DeBeer-Schmitt, P. A. Alekseev, J.-M. Mignot, S. M. Koohpayeh *et al.*, *Phys. Rev. Lett.* **114**, 036401 (2015).
- [20] G. A. Slack and S. Galginaitis, *Phys. Rev.* **133**, A253 (1964).
- [21] S. Y. Li, J.-B. Bonnemaïson, A. Payeur, P. Fournier, C. H. Wang, X. H. Chen, and L. Taillefer, *Phys. Rev. B* **77**, 134501 (2008).
- [22] S. Nakamura, T. Goto, M. Kasaya, and S. Kunii, *J. Phys. Soc. Jpn.* **60**, 4311 (1991).
- [23] H. Smith, G. Dolling, S. Kunii, M. Kasaya, B. Liu, K. Takegahara, T. Kasaya, and T. Goto, *Solid State Commun.* **53**, 15 (1985).
- [24] P. A. Popov, V. V. Novikov, A. A. Sidorov, and E. V. Maksimenko, *Inorganic Materials* **43**, 1187 (2007).
- [25] M. Hartstein, W. H. Toews, Y. T. Hsu, B. Zeng, X. Chen, M. C. Hatnean, Q. R. Zhang, S. Nakamura, A. S. Padgett, G. Rodway-Gant *et al.*, *Nat. Phys.* **14**, 166 (2017).