Tuning incommensurate charge order in Ba_{1-x}Sr_xAl₄ and Ba_{1-y}Eu_yAl₄

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(Received 7 May 2025; revised 25 June 2025; accepted 30 June 2025; published 21 July 2025)

The BaAl₄-type structure family is home to a vast landscape of interesting and exotic properties, with descendant crystal structures hosting a variety of electronic ground states including magnetic, superconducting, and strongly correlated electron phenomena. BaAl₄ itself hosts a nontrivial topological band structure, but is otherwise a paramagnetic metal. However, the other members of the AAl₄ family (A = alkali earth), including SrAl₄ and EuAl₄, exhibit symmetry-breaking ground states including charge density wave (CDW) and magnetic orders. Here we investigate the properties of the solid solution series Ba_{1-x}Sr_xAl₄ and Ba_{1-y}Eu_yAl₄ using transport, thermodynamic, and scattering experiments to study the evolution of the charge-ordered state as it is suppressed with Ba substitution to zero near 50% substitution in both systems. Neutron and x-ray diffraction measurements reveal an incommensurate CDW state in SrAl₄ with c-axis-oriented ordering vector (0, 0, 0.097) that evolves with Ba substitution toward a shorter wavelength. A similar progression is observed in the Ba_{1-y}Eu_yAl₄ series that also scales with the ordering temperature, revealing a universal correlation between charge-order transition temperature and ordering vector that points to a critical wave vector that stabilizes CDW order in both systems. We study the evolution of the phonon band structure in the Ba_{1-x}Sr_xAl₄ system, revealing that the suppression of the CDW phase matches the suppression of a phonon instability at precisely the same momentum as observed in experiments, confirming the electron-phonon origin of charge order in this system.

DOI: 10.1103/d8yy-1w31

I. INTRODUCTION

The evolution of interest in systems harboring chargeordered states has produced a plethora of fascinating phenomena and observations that shed light on both cooperative and competing states in a wide range of materials. Starting with the discovery and understanding of the role of charge order in the cuprate phase diagram [1], and more recently with the varieties of charge order in transition-metal dichalcogenides [2], time-reversal symmetry breaking at the charge-order transition in the kagome series AV₃Sb₅ [3], interplay with strong correlations in FeGe [4], and nematic order and fluctuations in BaNi₂As₂ [5], the interplay of charge, spin, and orbital degrees of freedom has come into focus as a key question in quantum materials. Additionally, the effect of charge modulation and symmetry breaking on topological aspects of electronic band structures has come to light as a potential area of interest, for instance in kagome materials [6], and charge-ordered phases have themselves been proposed to entail nontrivial topologies [7,8].

The family of materials with the BaAl₄ parent structure type hosts a variety of exotic behaviors [9], including iron-based superconductivity [10], heavy-fermion physics in

systems such as CeCu₂Si₂ [11], electronic nematic phases in BaNi₂As₂ [5], hidden order in URu₂Si₂ [12–14], and topological spin textures in EuGa₂Al₂ [15] and EuCd₂As₂ [16]. The AAl_4 and AGa_4 series of binary compounds—with A = Ba, Sr, Ca or Eu—have been known to harbor a variety of chargeordered and magnetic ground states [17,18], including charge density wave (CDW) order at 243 and 140 K in SrAl₄ and EuAl₄, respectively, and rare-earth magnetism below ∼20 K in the Eu-based compounds. However, recent studies of the BaAl₄ compound itself—a nonmagnetic, metallic material that does not exhibit any charge-ordered phase—have revealed it to host a crystalline symmetry-protected nontrivial topology with a three-dimensional Dirac spectrum [19,20] that likely also exists in the Sr- and Eu-based counterparts [21]. Charge order in SrAl₄ and EuAl₄, as well as its anomalous absence in the nearly identical BaAl4, have recently been studied theoretically [22] and experimentally [23–27], and debate about the origins of CDW order suggest a subtle sensitivity of the CDW phase to details of the phonon and electron band structures [22,26].

In this work, we study the evolution of the CDW state in the $Ba_{1-x}Sr_xAl_4$ and $Ba_{1-y}Eu_yAl_4$ solid solution series as a function of isovalent Sr/Eu substitution (x) in order to verify and

fully characterize the evolution of charge order with structural and electronic properties between the disparate end members, and to identify how CDW order appears with Sr and Eu substitution. Using single-crystal x-ray and neutron diffraction experiments, we characterize the CDW ordering q vector as a function of temperature and x for several characteristic concentrations through the range where CDW order is present in each series, to observe an evolution of the incommensurate q vector toward the complete suppression of CDW order near x = 0.50 in each case. We also performed x-ray diffraction experiments and ab initio density functional theory (DFT) calculations on the nonmagnetic $Ba_{1-x}Sr_xAl_4$ solid solution series to show how the minimal change in crystal structure with alkali-earth substitution has an impact on the phonon spectrum, resulting in an acoustic-mode instability that is suppressed in parallel with the observed CDW order. Our results are in good agreement with previous work suggesting CDW order in this series originates from a softened phonon mode and strong electron-phonon coupling, and provide detailed insight into how CDW order is universally fine tuned as a function of divalent cation substitution.

II. METHODS

Single crystals of $Ba_{1-x}Sr_xAl_4$ and $Ba_{1-y}Eu_yAl_4$ were grown using an Al self-flux method from elemental Ba, Eu, Sr, and Al (purities: 99%, 99.9%, 99%, and 99.999%, respectively) in a ratio of 1-x:x:16, with excess Al to act as a flux at high temperatures. The combination was placed in an alumina crucible and sealed inside a quartz tube in an argon atmosphere. The reaction mixture was heated to 1100 °C at 50 °C/hour, held at 1100 °C for 12 hours to homogenize the mixture, and slow cooled to 720 °C at 5 °C/hr before being put in a centrifuge to separate the flux from the crystals. This process resulted in large single crystals with dimensions exceeding $2 \times 2 \times 1$ mm³, with the shortest axis universally being the c axis, typical for tetragonal systems. Electrical transport measurements were made with a Quantum Design Physical Properties Measurement System (PPMS). For the transport measurements, gold wires were attached to the samples with DuPont 4929 silver paste.

Single-crystal x-ray diffraction at 250 K was collected on $Ba_{1-x}Sr_xAl_4$ and $Ba_{1-y}Eu_yAl_4$ samples with a Bruker APEX-II CCD system equipped with a graphite monochromator and a MoK α sealed tube ($\lambda = 0.71073$ Å). One sample (SrAl₄, UM No. 4008) was measured using a Bruker D8 Venture Duo diffractometer equipped with a Photon III detector, MoKa microfocus tube, and Helios optics, and all crystal-structure refinement was performed using the BRUKER SHELXTL software package [28]. Temperature-dependent single-crystal x-ray diffraction measurements were taken on Ba_{1-v}Eu_vAl₄ using a three-dimensional (3D) Mo K α (17.4 KeV) source, which delivers of the order of 10⁷ photons per second with a beam spot of 130 µm. The sample was cooled using a closed-cycle cryostat to reach a base temperature of 12 K. The sample was kept inside a Be dome, which was used for vacuum and radiation shielding. Sample motion was performed using a Huber four-circle diffractometer and x-ray detection was captured using a Mar345 image plate to allow for 3D mapping of momentum space with a resolution of q = 0.01 to

 0.08 Å^{-1} , depending on the cut. We transformed the data collected from real to reciprocal space over volumes in the range $V = 0.0007 - 0.003 \text{ Å}^{-3}$, depending on the zone of the Bragg peak. These volumes encompass the entire intensity of the CDW peak at base temperature and were kept constant (with increasing temperatures) for each substitution concentration.

Neutron diffraction measurements were performed with the BT-7 triple-axis spectrometer at the NIST Center for Neutron Research using a fixed incident wavelength $\lambda = 2.359 \text{ Å}$, horizontal collimations set to open -50' - 50' - 120' (full width at half maximum), pyrolytic graphite monochromator and analyzer, and pyrolytic graphite filters to suppress higherorder wavelengths [29]. A 57 mg single crystal of Sr_xAl₄ was aligned in the tetragonal (space group I4/mmm) [H, 0, L]scattering plane, where $a^* = 2\pi/a$ and $c^* = 2\pi/c$ with a =4.6424 Å and c = 11.2148 Å at 300 K. To reduce the possibility of introducing strain to the sample, we avoided using wire or glue for mounting. Instead, the crystal was mounted to an aluminum post by gently wrapping it with aluminum foil. A closed-cycle refrigerator with a base temperature of 5 K was used to control the sample temperature. Scans in reciprocal space were measured as a function of H and L on warming from 5 to 255 K. A very similar configuration was employed at the University of Missouri Research Reactor, with collimations of 60' - 60' - 40' - 40'. Uncertainties, where indicated throughout, represent one standard deviation.

III. EXPERIMENTAL RESULTS

We first discuss the effect of isovalent cation substitutions on the crystallographic structure of BaAl₄. As shown in Fig. 1, there is very minimal change in lattice parameters across both Sr- and Eu-substitution series. While the c/a ratio increases as expected due to the difference in cation radii, the unit cell only changes by \sim 1% along the crystallographic caxis across both Sr- and Eu-based series, which is a minute difference when compared to other similar Ba-Sr substitution series such as $Ba_{1-x}Sr_xFe_2As_2$ [30] and $Ba_{1-x}Sr_xNi_2As_2$ [5]. Geometric optimization calculations of the $Ba_{1-x}Sr_xAl_4$ experimental structures (performed to achieve less than 0.001 eV/Å force on each atom) yield relaxed structures that differ from the corresponding experimental a- and c-axis lattice constants by a maximum of 0.25% and 0.50%, respectively. Our calculations confirm the experimental findings that the crystal structures, e.g., c/a ratio, remain mostly unchanged with Ba-Sr substitution, suggesting that the Al substructure is quite rigid in this series and does not permit the usual chemical pressure effect of isovalent alkali-earth substitution, such as found, e.g., in $Ba_{1-x}Sr_xFe_2As_2$, or between $EuFe_2As_2$ and the Sr and Ba counterparts, where a much larger $\sim 10\%$ reduction in the *c*-axis unit-cell dimension is achieved [30,31]. This observation is one of the main motivations to try and understand the mechanism behind the strong tuning of CDW order with chemical substitution in the absence of large effects on crystallographic structure. Interestingly, the change in tetrahedral bond angles α and β evolves as expected for chemical pressure being applied to the tetragonal unit cell with Sr substitution, but with a much larger change than the Fe- and Ni-based examples, which only vary by $<1^{\circ}$ from x=0 to 1. This again reflects the dominance of the Al substructure.

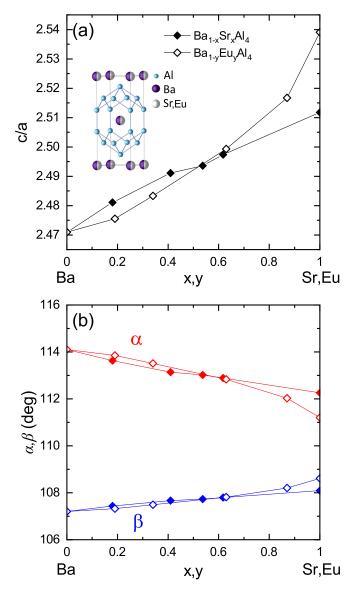


FIG. 1. Plot of quantities measured through x-ray experiments. (a) Plot of the ratio of the c axis to a axis. (b) The blue and red curves plot the angles α and β , respectively, which are the bond angles in the aluminum tetrahedron.

The metallic resistivity $\rho(T)$ of BaAl₄ and the related Srand Eu-based members is very similar in the paramagnetic, nonordered regimes. SrAl₄ exhibits metallic behavior on cooling, and the CDW transition T_{cdw} (x = 1), which appears as a kink in $\rho(T)$ at 235 K, can be tracked as a function of Ba substitution in $Ba_{1-x}Sr_xAl_4$, as shown in Fig. 2(a). Similarly, in Fig. 2(c), EuAl₄ exhibits metallic behavior upon cooling, followed by two distinct transitions: a CDW transition at 140 K and an antiferromagnetic transition at 15 K. The transitions in the Eu and Sr compounds are progressively suppressed with increasing Ba substitution, as evidenced by the shift in the temperature of the kink observed in $\rho(T)$. The alkali-earth substitution does not otherwise change the overall temperature behavior of $\rho(T)$, with the high-temperature linear slope nearly unchanged. The effect of substitution and the evolution of T_{cdw} can be clearly demonstrated by plotting the change in $\rho(T)$ as a function of x from the metallic parent compound BaAl₄, defined as

$$\Delta \rho = \frac{\rho_x(T) - \rho_x(2 \text{ K})}{\rho_x(300 \text{ K}) - \rho_x(2 \text{ K})} - \frac{\rho_0(T) - \rho_0(2 \text{ K})}{\rho_0(300 \text{ K}) - \rho_0(2 \text{ K})}.$$
 (1)

In this equation, ρ_x is the resistivity of the substituted sample and ρ_0 is the resistivity of BaAl₄. This normalizes the value of resistivity to lie between 0 and 1 and shows the magnitude of the deviation from the metallic resistivity of BaAl₄, where $T_{cdw} = 0$. The resultant phase diagram for Ba_{1-x}Sr_xAl₄ is presented in Fig. 2(b), which reflects the lack of change in $\rho(T)$ as a function of x. For Ba_{1-y}Eu_yAl₄, a similar trend is shown in Fig. 2(d), but with weaker deviations from the normalizing curve than for Ba_{1-x}Sr_xAl₄, Aside from the onset and evolution of CDW order, which will be discussed below, the near insensitivity of resistivity behavior to isovalent alkali-earth substitution is not surprising given the similar electronic band structures [17–20] in each end member and the dominant aluminum bands [22,26].

Despite such a small variation in lattice parameters, there is a strong evolution of CDW order with both Sr and Eu substitution, as shown in the phase diagrams of Fig. 2. The decrease in T_{cdw} with Ba substitution in both series is akin to the decrease observed as a function of pressure [17,32]. However, given the notable difference in crystallographic response noted above for alkali-earth substitution vs applied pressure, it is not clear that the mechanism is the same. Furthermore, in the substitution series, T_{cdw} appears to decrease over a wider temperature range before an abrupt drop near the midway point in substitution in both systems: $Ba_{1-x}Sr_xAl_4$ appears to show a discontinuous jump in T_{cdw} from zero to ~100 K near x = 0.5, and Ba_{1-v}Eu_vAl₄ also exhibits a jump close to y = 0.5. Lacking any abrupt changes in crystallographic parameters (cf. Fig. 1) in either system, this suggests the CDW phase itself approaches a critical point of instability. We will discuss this below.

To characterize the CDW distortion in these series, we performed x-ray and neutron diffraction measurements in the (h, 0, l) scattering plane for a series of substitutions through these series. Figure 3(a) shows neutron diffraction scans for SrAl₄ around (2,0,0) measured along $c^* = 2\pi/c$ [29]. At 5 K, large first-order satellites appear with approximately 30% of the intensity at the fundamental (2,0,0) Bragg peak. Scans in the a^* direction at q_{cdw} and $2q_{cdw}$ (not shown) demonstrate that the CDW peaks are strictly along c^* . In the ground state of SrAl₄, the modulation can be described with an incommensurate wave vector of the form $q_{cdw} = (0, 0, \eta)$ with $\eta =$ 0.097(3). The smoothly increasing temperature dependence makes the incommensurability clear. A second-order satellite indexed as $2q_{cdw}$ can be seen more clearly in the bottom plot of Fig. 3(a), which shows the same scan condition at several temperatures. Near 200 K, the intensity at $2q_{cdw}$ becomes unobservable above the background. The top plot of Fig. 3(a) displays the intensity map of scans along (2, 0, L), measured on warming for temperatures up to 255 K. The smooth evolution of the superlattice peaks away from (2,0,0) up to ~ 235 K confirms the incommensurability of the lattice distortion.

The CDW intensity for the primary CDW satellite peak, which is proportional to the square of the order parameter, is plotted in Fig. 3(b). These data were obtained from the

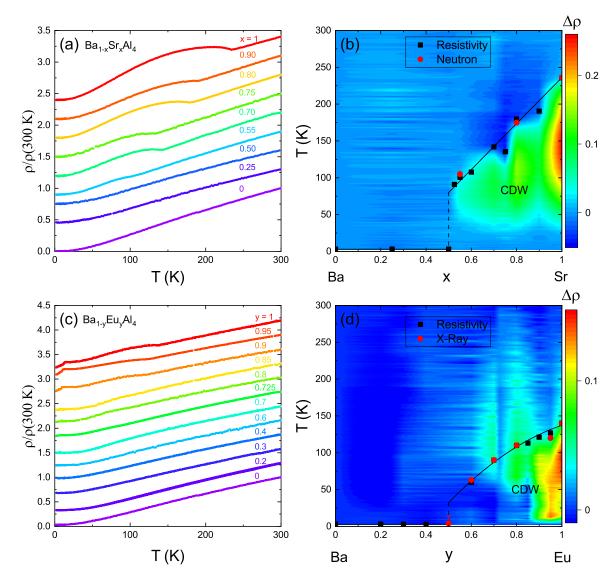


FIG. 2. (a), (c) Resistance curves of various substitutions of $Ba_{1-x}Sr_xAl_4$ and $Ba_{1-y}Eu_yAl_4$, respectively. The curves are normalized and stacked for easier interpretation. Suppression of the CDW transition is seen with hints of it in x = 0.55 substitution before disappearing at x = 0.5 in $Ba_{1-x}Sr_xAl_4$ and a similar suppression is seen around y = 0.4 in $Ba_{1-y}Eu_yAl_4$. (b) and (d) Phase diagrams of both substitution series, constructed using the resistivity difference $\Delta \rho$ from that of end members $BaAl_4$ and $EuAl_4$, respectively [see main text and Eq. (1)], and CDW transition temperature data obtained from resistivity, neutron, and x-ray diffraction data. The solid and dashed lines are guides to the eye.

integrated intensities of one of the satellite peaks extracted from the fits. A simple mean-field fit to the intensity at η versus T estimates an ordering temperature $T_{cdw}=236(3)$ K. The intensity of 2η falls off more rapidly, vanishing around 200 K. The wave vectors extracted from Gaussian fits of the (2,0,L) scans [bottom of Fig. 3(b)] show a smooth increase up to the phase transition. The results are consistent with a CDW with a single wave vector of the form ηq . We note that for metallic systems, the CDW wave vector is typically controlled by Fermi surface nesting and therefore does not show significant temperature dependence. This suggests that in the present system, either the Fermi surface exhibits a significant variation with temperature or q_{cdw} is not directly associated with the Fermi surface, but rather is controlled by competing interactions [33]. We will discuss this below.

To investigate the CDW evolution with cation substitutions, we repeated temperature-dependent neutron diffraction measurements for single crystals of $Ba_{1-x}Sr_xAl_4$ (x=0.55 and 0.80) and x-ray diffraction measurements of $Ba_{1-y}Eu_yAl_4$ (y=0.6,0.80, and 0.95). The resultant data for both series are summarized in Fig. 4, with integrated intensities plotted as a function of temperature in the same manner as above for the first-order CDW satellites. The CDW transition temperature decreases with larger Ba concentrations in both series down to $T_{cdw}=105(3)$ K for x=0.55, and 63 K for y=0.6, both just above the critical 50% onset concentration. More notably, in both series, Ba substitution causes an increase in the CDW wave vector of the form $q_{cdw}=(0,0,\eta)$, with η nearly doubling for both series, with progressive increases in η as T_{cdw} decreases. Presented in Fig. 5, this universal scaling, i.e.,

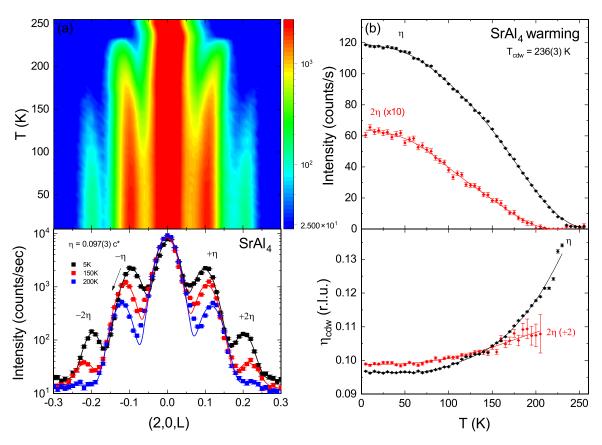


FIG. 3. Neutron diffraction along (2, 0, L) as a function of temperature for SrAl₄. (a) The top plot shows a contour map of the scattering intensity showing first- and second-order satellites around the fundamental Bragg peak. The lower plot shows scans at 5, 150, and 200 K on a logarithmic scale with Gaussian fits to yield $q_{cdw} = \eta c^*$, with $\eta = 0.097(3)$ in the ground state. (b) The top plots show the integrated intensity vs temperature extracted from Gaussian fits to the data. The black points represent the intensity of the primary (first-order) CDW order parameter and red points represent the second-order peak. A mean-field fit to the primary peaks gives a transition temperature of $T_{cdw} = 236(3)$ K, while the second-order peaks become unobservable above ~ 200 K. The bottom plot shows the temperature dependence of the first- and second-order wave vectors in reciprocal lattice units extracted from Gaussian fits. In principle, the data should overlap, with the small offset likely due to the overlapping peaks in the fits. The incommensurate wave vector increases smoothly and continuously with temperature up to T_{cdw} , with no evidence of any lock-in transitions.

 $\eta(T_{cdw})$, completely captures the evolution of incommensurability in both Sr- and Eu-based series, including the previously reported value $\eta=0.19$ for EuAl₄ with $T_{cdw}=140$ K [23]. This suggests that the correlation between T_{cdw} and η is a direct reflection of the driving mechanism of CDW order in this family. Note that while η remains clearly incommensurate across the series, its amplitude (not shown) does weaken with decreasing ordering temperature. Moreover, the trend in both Sr- and Eu-based series toward $T_{cdw}=0$ near $\eta\simeq0.23$ suggests an explanation for the abrupt drop in $T_{cdw}=0$ as a function of substitution in both systems (i.e., at x=0.5 and y=0.5; cf. Fig. 2).

IV. PHONON BAND STRUCTURE

A recent computational study [22] considered the origin of CDW order in the AAl_4 series, comparing the traditional Peierls-type Fermi surface nesting scenario [34] with a strong electron-phonon coupling scenario. Wang *et al.* found that the latter interaction leads to softening of the transverse acoustic (TA) mode that becomes imaginary at $q = 0.24(\pi/c)$, reported to be in good agreement with the original cited

value [17]. Here, we calculate the phonon dispersions for x = 0, 0.5, and 1, and compare them to Wang *et al.* and our experimental data.

DFT calculations were performed to obtain phonon dispersions using the finite-difference method for the three structures with experimental lattice parameters (for x = 0.50, we use the experimental lattice constants obtained for x =0.55). We used the Vienna ab initio simulation package (VASP) [35] + PHONOPY [36] implementations to calculate the phonon dispersions, with plane-wave basis set (cutoff of 650 eV) and projected augmented wave (PAW) pseudopotentials with Perdew, Burke, and Ernzerhof exchange-correlation functional including spin-orbit coupling (SOC). For the parent compounds, we have used a supercell of size $2 \times 2 \times 2$ of the primitive cell, and the convergence of the phonon bands was checked with respect to the k-point sampling $(14 \times 14 \times 14)$ with Gaussian smearing of width 0.05 eV. For the x = 0.50structure, a supercell of size $2 \times 2 \times 2$ of the conventional cell was used with k-point mesh size $10 \times 10 \times 4$.

The calculated phonon dispersions are plotted in Fig. 6 for x = 0, 0.5, and 1. In agreement with previous studies, we found no phonon instabilities in the parent compound BaAl₄.

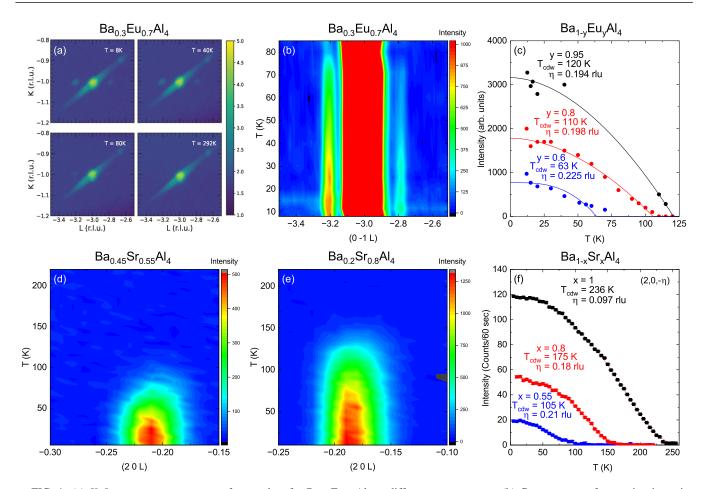


FIG. 4. (a) K, L momentum-space cut of x-ray data for Ba_{0.7}Eu_{0.3}Al₄ at different temperatures. (b) Contour map of scattering intensity showing satellite peaks around the Bragg peak in Ba_{0.7}Eu_{0.3}Al₄. (c) Intensity as a function of temperature for Ba_{1-x}Eu_xAl₄, where x = 0.95, 0.8, and 0.6. (d)–(f) Temperature dependence of the first-order CDW superlattice peaks for Ba_{1-x}Sr_xAl₄ (x = 0.55 and 0.8) measured with neutrons in the (H, 0, L) scattering plane. (d),(e) Contour plots of diffraction intensity for x = 0.8 and x = 0.55, respectively. The first-order peak shows y = 0.18 for y = 0.8 and y = 0.21 for y = 0.55. (f) Integrated intensity as a function of temperature extracted from Gaussian fits to the data for Ba_{1-x}Sr_xAl₄, where y = 1, 0.8 and 0.55.

For SrAl₄, there is a softening of the TA mode along the Γ -Z direction, with a minimum in the dispersion at $0.095(2\pi/c)$,

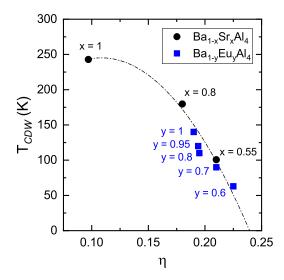


FIG. 5. T_{cdw} vs η for various members of the AAl₄ family. Values for EuAl₄ have been taken from [23].

consistent with the previous calculation which used a larger supercell [22], and in excellent agreement with $\eta=0.097$ obtained from the neutron diffraction data reported above. From our calculation for x=0.5, there are no unstable phonon modes present along the Γ -Z direction, although the frequency of the TA phonon mode at the Z point is lower compared to BaAl₄ and nearly similar to that of SrAl₄. The Γ -Z branch also clearly shows a flattening as compared to BaAl₄, suggesting that it is very near the onset of a softened mode. This is consistent with our experimental data, where η is also zero at x=0.5 but becomes finite (i.e., CDW order onsets) just above at x=0.55.

Intriguingly, all the calculated phonon spectra show a flat optical phonon band at the highest-frequency mode (9.8–11 THz). This band is doubly degenerate in the parent compounds and the degeneracy gets lifted in the substituted compounds due to the introduction of more than two distinct atomic positions for Al atoms. The flat band corresponds to modes which involve movement of only Al atoms in the c direction. This degeneracy gets lifted for the c = 0.5 case as the Al cage contains two types of center atoms, Ba or Sr.

V. DISCUSSION AND CONCLUSION

The insensitivity of the crystallographic structure to alkali-earth substitution in the AAl4 series makes the strong evolution of CDW order surprising in light of a seemingly unchanging chemical bonding environment. Furthermore, the stark similarities between CDW order in both Ba_{1-x}Sr_xAl₄ and Ba_{1-v}Eu_vAl₄ series, in particular the observed universal relation between ordering temperature T_{cdw} and ordering vector η (cf. Fig. 5), suggest an underlying mechanism that is rather independent of details of cation bonding or even magnetic interactions. Previous de Haas-van Alphen measurements [17] characterizing the Fermi surfaces of the AAl₄ series suggested that the Fermi surface of BaAl₄ is different from that of SrAl4, with the latter having a closer resemblance to that of its magnetic counterpart EuAl₄, leading Nakamura et al. to suggest the existence of a nesting wave vector in SrAl₄. However, recent calculations of the Fermi surfaces of BaAl₄ [19], SrAl₄, and EuAl₄ [22,26] have found that these are semimetals with nearly identical electronic environments, with strong spin-orbit coupling situating Dirac points in the spectra about 0.2–0.3 eV above the Fermi energy. Moreover, recent calculations of the band structure of SrAl₄ [22,26] have found an imperfect nesting, leading Wang et al. to the conclusion that strong electron-phonon coupling, rather than nesting, yields a softened TA phonon mode with small q vector along Γ -Z, explaining the origin of CDW order in the series [22]. This is in line with our findings, including both the calculated evolution of the TA modes and measured ordering wave vector through the $Ba_{1-x}Sr_xAl_4$ series, and suggests that the variation in the TA phonon mode stem from changes in the cation mass, nicely demonstrated by the continuous diminishing of CDW order with increasing the ratio of Ba to Sr and comparisons to EuAl₄ [24,26].

However, questions remain about CDW order and its sensitivity to atomic structure and substitution. Calculations by Ramakrishnan *et al.* indeed find an imperfect nesting in the electronic band structure of SrAl₄, but in contrast to the results of this study and Wang *et al.*, they did not identify any imaginary or soft modes attributable to the mechanism of CDW formation, concluding that the mechanism remains unknown [26].

Furthermore, while it has been known that the x=0 and x=1 end members of the $\mathrm{Ba}_{1-x}\mathrm{Sr}_x\mathrm{Al}_4$ series necessitate a transition between CDW and nonordered ground states at an intermediate concentration, our study reports an unexpected abrupt cutoff in the CDW phase near 50% substitution concentrations, observed in both series and consistent with the universal relation between ordering vector and temperature. Given that the assumed smooth variation of the TA phonon mode with changing cation mass is the driving force, an abrupt jump in the spectrum is not necessarily expected, suggesting either a percolation threshold is reached or another energy scale plays an intermediate role in the destabilization of CDW order. Considering that both the Sr- and Eu-based series show this instability at the same criticalc-axis ordering vector, the approach to this length scale warrants further investigation.

There are a few systems isostructural to $SrAl_4$ that harbor charge order and competing interactions. In particular, recent studies of the evolution of structural and charge order in the $Ba_{1-x}Sr_xNi_2As_2$ [5,37,38] have identified charge order

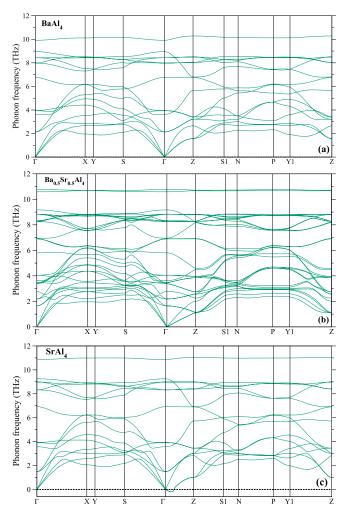


FIG. 6. Phonon dispersions for (a) $BaAl_4$, (b) $Ba_{0.5}Sr_{0.5}Al_4$, and (c) $SrAl_4$ along the Brillouin zone path of the corresponding primitive cells.

phases with similar temperature scales as SrAl₄. While these systems share an incommensurate nature, the NiAs-based system exhibits multiple coexisting CDW phases with much shorter wavelengths, and more important, strong correlations between structural distortions, CDW order, and electronic nematic fluctuations and ordered phases. Interestingly, the Ba_{1-r}Sr_rNi₂As₂ phase diagram exhibits an abrupt drop of its CDW order near 70% Sr, not unlike the discontinuous change near 50% in both $Ba_{1-x}Sr_xAl_4$ and $Ba_{1-y}Eu_yAl_4$, suggesting competing phases or intermediate energy scales may be playing a role in both cases. Regardless of the underlying mechanism of the first-order suppression of CDW order in the AAl₄ series reported here, it is interesting to consider the utility of this region of the phase diagram for tuning the electronic properties. Given the proven nontrivial topology of the electronic structures of both end members, this presents a unique ability to switch between the presence of CDW order while maintaining topological band structure, suggesting a different route to controlling the coupling of electronic interactions with band structure topology in a relatively inert and simple system.

Finally, a lower-temperature first-order transition near 90 K was previously observed in the electrical resistivity of $SrAl_4$ [17], but is not observed in our study of $Ba_{1-x}Sr_xAl_4$

single-crystal samples. This transition was recently reported to be a structural distortion from the high-temperature tetragonal phase to a monoclinic phase [26]. Because it was also reported that this distortion leaves the CDW order virtually unaffected, we do not believe it has significant consequences for our interpretations.

In this work, we have studied the structural and physical properties of the $Ba_{1-x}Sr_xAl_4$ and $Ba_{1-y}Eu_yAl_4$ solid solution series to investigate the evolution of charge density wave order with cation substitution up to its termination near 50% substitution in both series. Using neutron and x-ray diffraction measurements, we have determined the wave vectors of c-axis-oriented charge order to evolve smoothly in both series, ranging from $\eta = 0.097$ in SrAl₄ to $\eta 0.225$ in Ba_{0.4}Eu_{0.6}Al₄, with a common trend in both systems that intrinsically depends on the ordering temperature and is independent of the type of cation substitution. A comparison to phonon band calculations in Ba_{1-x}Sr_xAl₄ confirms a mechanism for CDW order stemming from softening of a transverse acoustic phonon mode with small wave vector along the Γ -Z direction, consistent with prior results [22]. This work provides a systematic insight into methods of controlling the coupling of electronic interactions with band structure topology in a simple, yet versatile platform.

ACKNOWLEDGMENTS

Research at the University of Maryland was supported by the Gordon and Betty Moore Foundation's EPiQS Initiative through Grant No. GBMF9071, the U.S. National Science Foundation Grant No. DMR2303090, the Binational Science Foundation Grant No. 2022126, and the Maryland Quantum Materials Center. S.B. and R.V. acknowledge support by the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) for funding through project TRR 288 -422213477 (Project No. A05). S.B. also acknowledges support from the U.S. National Science Foundation (NSF) Grant No. 2201516 under the Accelnet program of Office of International Science and Engineering (OISE). X-ray experiments were supported by the Center for Quantum Sensing and Quantum Materials under U.S. Department of Energy BES Award No. DE-SC0021238. P.A. acknowledges support from the EPiQS program of the Gordon and Betty Moore Foundation, Grant No. GBMF9452. The identification of any commercial product or trade name does not imply endorsement or recommendation by the National Institute of Standards and Technology.

DATA AVAILABILITY

The data that support the findings of this article are not publicly available upon publication because it is not technically feasible and/or the cost of preparing, depositing, and hosting the data would be prohibitive within the terms of this research project. The data are available from the authors upon reasonable request.

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